

# Package: ARCokrig (via r-universe)

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**Type** Package

**Title** Autoregressive Cokriging Models for Multifidelity Codes

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**Description** For emulating multifidelity computer models. The major methods include univariate autoregressive cokriging and multivariate autoregressive cokriging. The autoregressive cokriging methods are implemented for both hierarchically nested design and non-nested design. For hierarchically nested design, the model parameters are estimated via standard optimization algorithms; For non-nested design, the model parameters are estimated via Monte Carlo expectation-maximization (MCEM) algorithms. In both cases, the priors are chosen such that the posterior distributions are proper. Notice that the uniform priors on range parameters in the correlation function lead to improper posteriors. This should be avoided when Bayesian analysis is adopted. The development of objective priors for autoregressive cokriging models can be found in Pulong Ma (2020) <[DOI:10.1137/19M1289893](https://doi.org/10.1137/19M1289893)>. The development of the multivariate autoregressive cokriging models with possibly non-nested design can be found in Pulong Ma, Georgios Karagiannis, Bledar A Konomi, Taylor G Asher, Gabriel R Toro, and Andrew T Cox (2019) <[arXiv:1909.01836](https://arxiv.org/abs/1909.01836)>.

**License** GPL (>= 2)

**Encoding** UTF-8

**URL** <https://github.com/pulongma/ARCokrig/issues>

**Depends** R (>= 3.5.0)

**Imports** Rcpp, mvtnorm (>= 1.0-10), stats, methods, ggplot2

**LinkingTo** Rcpp, RcppArmadillo, RcppEigen

**RoxygenNote** 6.1.1

**Repository** <https://pulongma.r-universe.dev>  
**RemoteUrl** <https://github.com/pulongma/arcokrig>  
**RemoteRef** HEAD  
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ARCoKrig	<i>Fit the AR-Cokriging model and make predictions</i>
----------	--

---

**Description**

This is a simple and high-level function to fit autoregressive cokriging models to multifidelity computer model outputs.

**Usage**

```
ARCoKrig(  
  formula = list(~1, ~1),  
  output,  
  input,  
  cov.model = "matern_5_2",  
  nugget.est = FALSE,  
  input.new,  
  prior = list(),  
  opt = list(),  
  NestDesign = TRUE,  
  tuning = list(),  
  info = list()  
)
```

**Arguments**

formula	a list of $s$ elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of $s$ elements, each of which contains a matrix of computer model outputs.
input	a list of $s$ elements, each of which contains a matrix of inputs.
cov.model	a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include <b>exp</b> product form of exponential covariance functions. <b>matern_3_2</b> product form of Matern covariance functions with smoothness parameter $3/2$ . <b>matern_5_2</b> product form of Matern covariance functions with smoothness parameter $5/2$ . <b>Gaussian</b> product form of Gaussian covariance functions. <b>powexp</b> product form of power-exponential covariance functions with roughness parameter fixed at 1.9.
nugget.est	a logical value indicating whether nugget parameter is included or not. Default value is FALSE.
input.new	a matrix including new inputs for making prediction
prior	a list of arguments to setup the prior distributions <b>name</b> the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys <b>hyperparam</b> hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: $a$ refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; $b$ refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).
opt	a list of arguments to setup the <b>optim</b> routine.
NestDesign	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.
tuning	a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments <b>maxit</b> the maximum number of MCEM iterations. <b>tol</b> a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped. <b>n.sample</b> the number of Monte Carlo samples in the MCEM algorithm. <b>verbose</b> a logical value to show the MCEM iterations if it is true.
info	a list that contains <b>iter</b> number of iterations used in the MCEM algorithm <b>eps</b> parameter difference after the MCEM algorithm stops

**Value**

The main call inside `ARCokrig` consists of `cokm`, `cokm.fit`, and `cokm.predict`. Thus, the function returns the `cokm` object and predictions over new inputs.

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**References**

- Ma, P. (2019). "Objective Bayesian Analysis of a Cokriging Model for Hierarchical Multifidelity Codes." arXiv:1910.10225. <https://arxiv.org/abs/1910.10225>.
- Ma, P., Karagiannis, G., Konomi, B., Asher, T., Toro, G., and Cox, A. (2019) "Multifidelity Computer Model Emulation with High-Dimensional Output: An Application to Storm Surge." arXiv:1909.01836. <https://arxiv.org/abs/1909.01836>.

**See Also**

`cokm`, `cokm.param`, `cokm.fit`, `cokm.predict`

**Examples**

```
#####
#####
##### Example
Funcc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funcc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funcc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## fit and predict with the AR-Cokriging model

out = ARCokrig(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
               input=list(as.matrix(Dc), as.matrix(Df)),
```

```

cov.model="matern_5_2",
input.new=input.new)

## plot results

library(ggplot2)
cokrig = out$cokrig
df.l1 = data.frame(x=c(Dc), y=c(zc))
df.l2 = data.frame(x=c(Df), y=c(zf))
CI.lower = cokrig$lower95[[2]]
CI.upper = cokrig$upper95[[2]]
df.CI = data.frame(x=c(input.new), lower=CI.lower, upper=CI.upper)
df.pred = data.frame(x=c(input.new), y=cokrig$mu[[2]])

g = ggplot(data.frame(x=c(-1,1)), aes(x)) +
  stat_function(fun=Func, geom="line", aes(colour="level 1"), n=500) +
  stat_function(fun=Funcf, geom="line", aes(colour="level 2"), n=500)

g = g + geom_point(data=df.l1, mapping=aes(x=x, y=y), shape=16, size=2, color="black") +
  geom_point(data=df.l2, mapping=aes(x=x, y=y), shape=17, size=2, color="black")

g = g + geom_line(data=df.pred, aes(x=x, y=y, colour="cokriging"), inherit.aes=FALSE) +
  geom_ribbon(data=df.CI, mapping=aes(x=x, ymin=lower, ymax=upper), fill="gray40",
    alpha=0.3, inherit.aes=FALSE)
g = g + scale_colour_manual(name=NULL, values=c("red", "blue", "turquoise3"),
  breaks=c("cokriging", "level 1", "level 2"))

g = g + ggtitle("A Two-Level Example") +
  theme(plot.title=element_text(size=14),
    axis.title.x=element_text(size=14),
    axis.text.x=element_text(size=14),
    axis.title.y=element_text(size=14),
    axis.text.y=element_text(size=14),
    legend.text = element_text(size=12),
    legend.direction = "horizontal",
    legend.position = c(0.6, 0.1)) + xlab("") + ylab("")
print(g)

```

---

cokm

---

*Construct the cokm object*


---

## Description

This function constructs the cokm object in autogressive cokriging models

**Usage**

```
cokm(
  formula = list(~1, ~1),
  output,
  input,
  cov.model = "matern_5_2",
  nugget.est = FALSE,
  prior = list(),
  opt = list(),
  NestDesign = TRUE,
  tuning = list(),
  info = list()
)
```

**Arguments**

formula	a list of $s$ elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of $s$ elements, each of which contains a matrix of computer model outputs.
input	a list of $s$ elements, each of which contains a matrix of inputs.
cov.model	a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include <b>exp</b> product form of exponential covariance functions. <b>matern_3_2</b> product form of Matern covariance functions with smoothness parameter $3/2$ . <b>matern_5_2</b> product form of Matern covariance functions with smoothness parameter $5/2$ . <b>Gaussian</b> product form of Gaussian covariance functions. <b>powexp</b> product form of power-exponential covariance functions with roughness parameter fixed at 1.9.
nugget.est	a logical value indicating whether the nugget is included or not. Default value is FALSE.
prior	a list of arguments to setup the prior distributions with the reference prior as default. <b>name</b> the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys <b>hyperparam</b> hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: $a$ refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; $b$ refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).
opt	a list of arguments to setup the <b>optim</b> routine.
NestDesign	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.

tuning	<p>a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments</p> <p><b>maxit</b> the maximum number of MCEM iterations.</p> <p><b>tol</b> a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.</p> <p><b>n.sample</b> the number of Monte Carlo samples in the MCEM algorithm.</p> <p><b>verbose</b> a logical value to show the MCEM iterations if it is true.</p>
info	<p>a list that contains</p> <p><b>iter</b> number of iterations used in the MCEM algorithm</p> <p><b>eps</b> parameter difference after the MCEM algorithm stops</p>

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[ARCokrig](#), [cokm.fit](#), [cokm.predict](#)

---

cokm-class

*cokm Class*


---

**Description**

This is an S4 class definition for [cokm](#) in the [ARCokrig](#) package

**Slots**

**output** a list of  $s$  elements, each of which contains a matrix of computer model outputs.

**input** a list of  $s$  elements, each of which contains a matrix of inputs.

**param** a list of  $s$  elements, each of which contains a vector of initial values for correlation parameters (and nugget variance parameters if nugget terms are included in AR-cokriging models).

**cov.model** a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include

- exp** product form of exponential covariance functions.
- matern\_3\_2** product form of Matern covariance functions with smoothness parameter  $3/2$ .
- matern\_5\_2** product form of Matern covariance functions with smoothness parameter  $5/2$ .
- Gaussian** product form of Gaussian covariance functions.
- powexp** product form of power-exponential covariance functions with roughness parameter fixed at 1.9.

**nugget.est** a logical value indicating whether nugget parameter is included or not. Default value is FALSE.

**prior** a list of arguments to setup the prior distributions with the reference prior as default

**name** the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind\_Jeffreys

**hyperparam** hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included:  $a$  refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2;  $b$  refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).

**opt** a list of arguments to setup the `optim` routine.

**NestDesign** a logical value indicating whether the experimental design is hierarchically nested within each level of the code.

**tuning** a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments

**maxit** the maximum number of MCEM iterations.

**tol** a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.

**n.sample** the number of Monte Carlo samples in the MCEM algorithm.

**verbose** a logical value to show the MCEM iterations if it is true.

**info** a list that contains

**iter** number of iterations used in the MCEM algorithm

**eps** parameter difference after the MCEM algorithm stops.

#### Author(s)

Pulong Ma <mpulong@gmail.com>

---

cokm.condsim	<i>Conditional simulation at new inputs in the autoregressive cokriging model</i>
--------------	---

---

#### Description

This function simulate from predictive distributions in autoregressive cokriging models

#### Usage

```
cokm.condsim(obj, input.new, nsample = 30)
```

#### Arguments

<code>obj</code>	a <code>cokm</code> object constructed via the function <code>cokm</code> in this package
<code>input.new</code>	a matrix including new inputs for making prediction
<code>nsample</code>	a numerical value indicating the number of samples



**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[cokm](#), [cokm.fit](#), [cokm.predict](#), [ARCokrig](#)

**Examples**

```

Funcc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funcc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

##### Nested design #####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funcc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="Reference")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
            input=list(as.matrix(Dc), as.matrix(Df)),
            prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)

cokrige = cokm.condsim(obj, input.new, nsample=30)

```

**Description**

This function estimates parameters in autogressive cokriging models

**Usage**

```
cokm.fit(obj)
```

**Arguments**

obj                    a [cokm](#) object constructed via the function [cokm](#) in this package

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[cokm](#), [cokm.param](#), [cokm.predict](#), [ARCoKrig](#)

**Examples**

```
Funcc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funcc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funcc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="JR")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
           input=list(as.matrix(Dc), as.matrix(Df)),
           prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)
```

---

cokm.param

*Get model parameters in the autoregressive cokriging model*


---

### Description

This function compute estimates for regression and variance parameters given the correlation parameters are known. It is used to show all model parameters in one place.

### Usage

```
cokm.param(obj)
```

### Arguments

obj                    a [cokm](#) object construted via the function [cokm](#) in this package

### Value

a list of model parameters including regression coefficients  $\beta$ , scale discrepancy  $\gamma$ , variance parameters  $\sigma^2$ , and correlation parameters  $\phi$  in covariance functions. If nugget parameters are included in the model, then nugget parameters are shown in  $\phi$ .

### Author(s)

Pulong Ma <mpulong@gmail.com>

### See Also

[cokm](#), [cokm.fit](#), [cokm.condsim](#), [ARCokrig](#)

---

cokm.predict

*Prediction at new inputs in the autoregressive cokriging model*


---

### Description

This function makes prediction in autogressive cokriging models. If a nested design is used, the predictive mean and predictive variance are computed exactly; otherwise, Monte Carlo simulation from the predictive distribution is used to approximate the predictive mean and predictive variance.

### Usage

```
cokm.predict(obj, input.new)
```

**Arguments**

`obj` a `cokm` object constructed via the function `cokm` in this package  
`input.new` a matrix including new inputs for making prediction

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

`cokm`, `cokm.fit`, `cokm.condsim`, `ARCokrig`

**Examples**

```
Funcc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funcc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funcc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="Reference")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
            input=list(as.matrix(Dc), as.matrix(Df)),
            prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)

cokrige = cokm.predict(obj, input.new)
```

---

CRPS

---

*Compute continous rank probability score for normal distributions*


---

**Description**

This function compute the continous rank probability score for normal distributions. It is mainly used to evaluate the validity of predictive distributions.

**Usage**

```
CRPS(x, mu, sig)
```

**Arguments**

x	a vector of true values (held-out data)
mu	a vector of predictive means
sig	a vector of predictive standard deviations

**Author(s)**

Pulong Ma <mpulong@gmail.com>

---

mvcokm

---

*Construct the mvcokm object*


---

**Description**

This function constructs the mvcokm object in autogressive cokriging models for multivariate outputs. The model is known as the parallel partial (PP) cokriging emulator.

**Usage**

```
mvcokm(
  formula = list(~1, ~1),
  output,
  input,
  cov.model = "matern_5_2",
  nugget.est = FALSE,
  prior = list(),
  opt = list(),
  NestDesign = TRUE,
  tuning = list(),
  info = list()
)
```

**Arguments**

formula	a list of $s$ elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of $s$ elements, each of which contains a matrix of computer model outputs.
input	a list of $s$ elements, each of which contains a matrix of inputs.
cov.model	<p>a string indicating the type of covariance function in the PP cokriging models. Current covariance functions include</p> <p><b>exp</b> product form of exponential covariance functions.</p> <p><b>matern_3_2</b> product form of Matern covariance functions with smoothness parameter <math>3/2</math>.</p> <p><b>matern_5_2</b> product form of Matern covariance functions with smoothness parameter <math>5/2</math>.</p> <p><b>Gaussian</b> product form of Gaussian covariance functions.</p> <p><b>powexp</b> product form of power-exponential covariance functions with roughness parameter fixed at 1.9.</p>
nugget.est	a logical value indicating whether the nugget is included or not. Default value is FALSE.
prior	<p>a list of arguments to setup the prior distributions with the jointly robust prior as default</p> <p><b>name</b> the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys</p> <p><b>hyperparam</b> hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: <math>a</math> refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; <math>b</math> refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).</p>
opt	a list of arguments to setup the <b>optim</b> routine.
NestDesign	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.
tuning	<p>a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments</p> <p><b>maxit</b> the maximum number of MCEM iterations.</p> <p><b>tol</b> a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.</p> <p><b>n.sample</b> the number of Monte Carlo samples in the MCEM algorithm.</p> <p><b>verbose</b> a logical value to show the MCEM iterations if it is true.</p>
info	<p>a list that contains</p> <p><b>iter</b> number of iterations used in the MCEM algorithm</p> <p><b>eps</b> parameter difference after the MCEM algorithm stops</p>

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[ARCokrig](#), [mvcokm.fit](#), [mvcokm.predict](#), [mvcokm.condsim](#)

---

mvcokm-class

*mvcokm Class*


---

**Description**

This is an S4 class definition for [mvcokm](#) in the [ARCokrig](#) package

**Slots**

**output** a list of  $s$  elements, each of which contains a matrix of computer model outputs.

**input** a list of  $s$  elements, each of which contains a matrix of inputs.

**param** a list of  $s$  elements, each of which contains a vector of initial values for correlation parameters (and nugget variance parameters if nugget terms are included in AR-cokriging models).

**cov.model** a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include

**exp** product form of exponential covariance functions.

**matern\_3\_2** product form of Matern covariance functions with smoothness parameter  $3/2$ .

**matern\_5\_2** product form of Matern covariance functions with smoothness parameter  $5/2$ .

**Gaussian** product form of Gaussian covariance functions.

**powexp** product form of power-exponential covariance functions with roughness parameter fixed at 1.9.

**aniso\_exp** anisotropic form of exponential covariance function.

**aniso\_matern\_3\_2** anisotropic form of Matern covariance functions with smoothness parameter  $3/2$ .

**aniso\_matern\_5\_2** anisotropic form of Matern covariance functions with smoothness parameter  $5/2$ .

**nugget.est** a logical value indicating whether the nugget is included or not. Default value is FALSE.

**prior** a list of arguments to setup the prior distributions with the jointly robust prior as default

**name** the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind\_Jeffreys

**hyperparam** hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included:  $a$  refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2;  $b$  refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support  $(0, 1)$ .

**opt** a list of arguments to setup the [optim](#) routine.

**NestDesign** a logical value indicating whether the experimental design is hierarchically nested within each level of the code.

**tuning** a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments

- maxit** the maximum number of MCEM iterations.
- tol** a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.
- n.sample** the number of Monte Carlo samples in the MCEM algorithm.

**info** a list that contains

- iter** number of iterations used in the MCEM algorithm
- eps** parameter difference after the MCEM algorithm stops

#### Author(s)

Pulong Ma <mpulong@gmail.com>

---

mvcokm.condsim	<i>Conditional simulation at new inputs in autoregressive cokriging models for multivariate output</i>
----------------	--

---

#### Description

This function makes prediction based on conditional simulation in autoregressive cokriging models for multivariate output

#### Usage

```
mvcokm.condsim(obj, input.new, nsample = 30)
```

#### Arguments

<b>obj</b>	a <a href="#">mvcokm</a> object constructed via the function <a href="#">mvcokm</a> in this package
<b>input.new</b>	a matrix including new inputs for making prediction
<b>nsample</b>	a numerical value indicating the number of samples

#### Author(s)

Pulong Ma <mpulong@gmail.com>

#### See Also

[mvcokm](#), [mvcokm.fit](#), [mvcokm.predict](#), [ARCoKrig](#)



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mvcokm.fit	<i>fit the autoregressive cokriging model for multivariate output</i>
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---

**Description**

This function estimates parameters in the parallel partial cokriging model

**Usage**

```
mvcokm.fit(obj)
```

**Arguments**

obj                    a [mvcokm](#) object constructed via the function [mvcokm](#) in this package

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[mvcokm](#), [mvcokm.predict](#), [mvcokm.condsim](#), [ARCokrig](#)

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mvcokm.param	<i>Get model parameters in autoregressive cokriging models for multivariate output</i>
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---

**Description**

This function computes estimates for regression and variance parameters given the correlation parameters are known. It is used to show all model parameters in one place.

**Usage**

```
mvcokm.param(obj)
```

**Arguments**

obj                    a [mvcokm](#) object constructed via the function [mvcokm](#) in this package

**Value**

a list of model parameters including regression coefficients  $\beta$ , scale discrepancy  $\gamma$ , variance parameters  $\sigma^2$ , and correlation parameters  $\phi$  in covariance functions. If nugget parameters are included in the model, then nugget parameters are shown in  $\phi$ .

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[mvcokm](#), [mvcokm.fit](#), [mvcokm.predict](#), [ARCokrig](#)

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`mvcokm.predict`

*Prediction at new inputs in autoregressive cokriging models for multi-variate output*

---

**Description**

This function makes prediction in the parallel partial cokriging model. If a nested design is used, the predictive mean and predictive variance are computed exactly; otherwise, Monte Carlo simulation from the predictive distribution is used to approximate the predictive mean and predictive variance.

**Usage**

```
mvcokm.predict(obj, input.new)
```

**Arguments**

<code>obj</code>	a <a href="#">mvcokm</a> object constructed via the function <a href="#">mvcokm</a> in this package
<code>input.new</code>	a matrix including new inputs for making prediction

**Author(s)**

Pulong Ma <mpulong@gmail.com>

**See Also**

[mvcokm](#), [mvcokm.fit](#), [mvcokm.condsim](#), [ARCokrig](#)

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